

Probing Gluon TMDs at a Future EIC

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Gluon TMDs can be accessed through the analysis of azimuthal asymmetries for heavy quark pair and dijet production in electron-proton collisions, similarly to the way quark TMDs are commonly extracted from semi-inclusive deep-inelastic scattering data. We calculate the upper bounds for these observables, showing in which kinematic regions they are large enough to be measured in future experiments at an Electron-Ion Collider. Moreover, we study their behavior in the small- x region, adopting a McLerran-Venugopalan model for unpolarized and linearly polarized gluon distributions. By comparison with related observables at RHIC and LHC, we expect to gather information on the process dependence of the gluon TMDs and to test our prediction of a sign change of the gluon Sivers function and two other T -odd gluon distributions.

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1. Introduction

Transverse momentum dependent parton distribution functions (TMDs) encode fundamental information on the intrinsic motion of partons and the correlation between their spins and momenta, providing a full three-dimensional picture of the proton in momentum space. While much effort has been made in order to extract quark TMDs, mainly from low energy data on semi-inclusive deep inelastic scattering (SIDIS), almost nothing is known experimentally about gluon TMDs.

In case of unpolarized protons, in addition to the unpolarized gluon TMD, the distribution of linearly polarized gluons is of special interest [1]: it corresponds to an interference between $+1$ and -1 gluon helicity states and, being T -even, it can in principle be nonzero even in absence of initial (ISI) and final state interactions (FSI). However this distribution, like all other TMDs, is affected by such interactions that can render it process dependent. For a transversely polarized proton, exactly in the same way as for quarks, it is possible to define a T -odd Sivers function for unpolarized gluons [2, 3], which describes their azimuthal distribution and might give rise to sizable left-right asymmetries. Furthermore, there are two other independent T -odd gluon TMDs: both of them are helicity-flip distributions of linearly polarized gluons.

In this contribution to the proceedings, after providing the definition of gluon TMDs in terms of QCD operators, we show how they can be probed directly by looking at transverse single spin and azimuthal asymmetries in both heavy quark pair and dijet production in electron-proton collisions [4, 5, 6]. Moreover, we discuss their process dependence and behavior in the small- x regime. A test of our predictions would be possible at a future Electron-Ion Collider (EIC) [7] where both the small and large x regions can be accessed. We suggest related measurements in proton-proton collisions that could be performed at RHIC and the LHC, where a possible fixed target experiment, called AFTER@LHC [8], would allow to investigate the structure of transversely polarized protons as well. A consistent picture among the various processes, at large and small x , will confirm our understanding of transverse spin effects and the TMD formalism in general.

2. Definition of gluon TMDs

We consider a gluon that carries momentum p inside a proton with momentum P and spin vector S . If we introduce a light-like vector n conjugate to P , the longitudinal and transverse components of gluon momentum can be defined via the Sudakov decomposition $p = xP + p_T + p^-n$. Similarly, the spin vector of the proton can be written as

$$S^\mu = \frac{S_L}{M_p} \left(P^\mu - \frac{M_p^2}{P \cdot n} n^\mu \right) + S_T^\mu, \quad (2.1)$$

where $S_L^2 + S_T^2 = 1$ and M_p is the proton mass. Gluon TMDs are defined through the following correlator [1],

$$\Gamma_g^{\mu\nu}(x, \mathbf{p}_T) = \frac{n_p n_\sigma}{(P \cdot n)^2} \int \frac{d(\xi \cdot P) d^2 \xi_T}{(2\pi)^3} e^{ip \cdot \xi} \langle P, S | \text{Tr} [F^{\mu\rho}(0) U_{[0,\xi]} F^{\nu\sigma}(\xi) U'_{[\xi,0]}] | P, S \rangle \rangle_{\text{LF}}, \quad (2.2)$$

with the gluon field strengths $F^{\mu\nu}(0)$ and $F^{\nu\sigma}(\xi)$ evaluated at a fixed light-front (LF) time $\xi^+ = \xi \cdot n = 0$. The process dependent Wilson lines or gauge links $U_{[0,\xi]}$ and $U'_{[0,\xi]}$ in Eq. (2.2) encode

the effects of ISI/FSI and are needed to ensure gauge invariance. Introducing the symmetric and antisymmetric transverse projectors, $g_T^{\mu\nu} = g^{\mu\nu} - P^\mu n^\nu / P \cdot n - n^\mu P^\nu / P \cdot n$ and $\varepsilon_T^{\mu\nu} = \varepsilon_T^{\alpha\beta\mu\nu} P_\alpha n_\beta / P \cdot n$ (with $\varepsilon_T^{12} = +1$), the correlator for an unpolarized (U) can be parametrized in terms of gluon TMDs as follows,

$$\Gamma_U^{\mu\nu}(x, \mathbf{p}_T) = \frac{x}{2} \left\{ -g_T^{\mu\nu} f_1^g(x, \mathbf{p}_T^2) + \left(\frac{p_T^\mu p_T^\nu}{M_p^2} + g_T^{\mu\nu} \frac{\mathbf{p}_T^2}{2M_p^2} \right) h_1^{\perp g}(x, \mathbf{p}_T^2) \right\}, \quad (2.3)$$

where f_1^g is the unpolarized gluon TMD and $h_1^{\perp g}$ is the distribution of linearly polarized gluons. Analogously, for a transversely polarized (T) proton,

$$\begin{aligned} \Gamma_T^{\mu\nu}(x, \mathbf{p}_T) = \frac{x}{2} \left\{ g_T^{\mu\nu} \frac{\varepsilon_T^{\rho\sigma} p_{T\rho} S_{T\sigma}}{M_p} f_{1T}^{\perp g}(x, \mathbf{p}_T^2) + i \varepsilon_T^{\mu\nu} \frac{p_T \cdot S_T}{M_p} g_{1T}^g(x, \mathbf{p}_T^2) \right. \\ \left. + \frac{p_{T\rho} \varepsilon_T^{\rho\{\mu} p_T^{\nu\}}}{2M_p^2} \frac{p_T \cdot S_T}{M_p} h_{1T}^{\perp g}(x, \mathbf{p}_T^2) - \frac{p_{T\rho} \varepsilon_T^{\rho\{\mu} S_T^{\nu\}} + S_{T\rho} \varepsilon_T^{\rho\{\mu} p_T^{\nu\}}}{4M_p} h_{1T}^g(x, \mathbf{p}_T^2) \right\} \end{aligned} \quad (2.4)$$

where $f_{1T}^{\perp g}$ is the T -odd gluon Sivers function. The distributions $h_{1T}^{\perp g}$ and h_{1T}^g , which are T -odd as well, are named in analogy with the quark ones [9], although quark and gluon TMDs with the same name have different properties under symmetry operations. The h functions for quarks are chiral-odd and do not mix with the chiral-even h functions for gluons. These distributions have to satisfy the following positivity bounds [1]

$$\frac{|\mathbf{p}_T|}{M_p} |f_{1T}^{\perp g}(x, \mathbf{p}_T^2)| \leq f_1^g(x, \mathbf{p}_T^2), \quad \frac{|\mathbf{p}_T|}{M_p} |h_{1T}^g(x, \mathbf{p}_T^2)| \leq f_1^g(x, \mathbf{p}_T^2), \quad \frac{|\mathbf{p}_T|^3}{2M_p^3} |h_{1T}^{\perp g}(x, \mathbf{p}_T^2)| \leq f_1^g(x, \mathbf{p}_T^2), \quad (2.5)$$

where we have defined the combination $h_1^g \equiv h_{1T}^g + \mathbf{p}_T^2 / (2M_p^2) h_{1T}^{\perp g}$, which is not related to the well-known transversity distribution h_1^q for quarks that has no analogue in the gluon sector. This notation is justified by the fact that both h_1^q and h_1^g denote helicity flip distributions. Moreover, we will show that they can give rise to the same angular dependences in different types of processes. However, h_1^q is chiral-odd, T -even, and survives after transverse momentum integration, whereas h_1^g is chiral-even, T -odd, and vanishes when integrated over transverse momentum.

3. Azimuthal asymmetries for heavy quark pair and dijet production in DIS

We first consider the process $e(\ell) + p(P, S) \rightarrow e(\ell') + Q(K_1) + \bar{Q}(K_2) + X$, where the proton has polarization vector S and the other particles are unpolarized. We fix a reference frame such that the \hat{z} -axis is along the direction of the proton and the virtual photon exchanged in the reaction, while the azimuthal angles are measured w.r.t. the lepton plane ($\phi_\ell = \phi_{\ell'} = 0$). In the so-called correlation limit, the two heavy quarks with transverse momenta $K_{i\perp}$ ($i = 1, 2$) such that $K_{i\perp}^2 = -\mathbf{K}_{i\perp}^2$, are almost back to back in the plane orthogonal to \hat{z} . Hence, if we define $q_T \equiv K_{1\perp} + K_{2\perp}$ and $K_\perp \equiv (K_{1\perp} - K_{2\perp})/2$, we have $|q_T| \ll |K_\perp|$. Denoting by ϕ_S , ϕ_T and ϕ_\perp the azimuthal angles

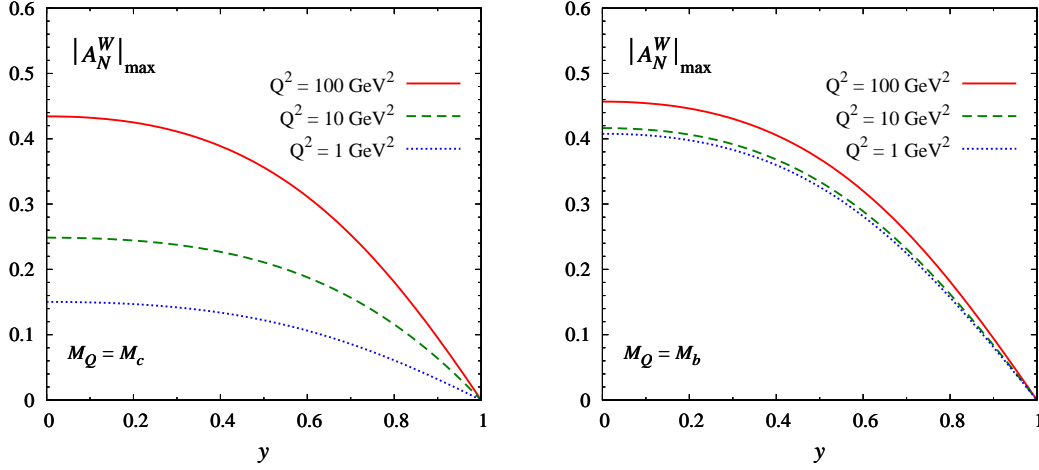


Figure 1: Upper bounds $|A_N^W|_{\max}$ on the asymmetries $A_N^{\sin(\phi_S+\phi_T)}$ and $A_N^{\sin(\phi_S-3\phi_T)}$ for the processes $ep \rightarrow e'c\bar{c}X$ (left panel) and $ep \rightarrow e'b\bar{b}X$ (right panel). Estimates are given as a function of y , at $z = 0.5$ and fixed values of Q^2 and $K_\perp (> 1 \text{ GeV})$, the latter chosen in such a way that the asymmetries are maximal.

of the three-vectors \mathbf{S}_T , \mathbf{q}_T and \mathbf{K}_\perp , the cross section at leading order in perturbative QCD can be written in the following form

$$\frac{d\sigma}{dy_1 dy_2 dy dx_B d^2\mathbf{q}_T d^2\mathbf{K}_\perp} \equiv d\sigma(\phi_S, \phi_T, \phi_\perp) = d\sigma^U(\phi_T, \phi_\perp) + d\sigma^T(\phi_S, \phi_T, \phi_\perp), \quad (3.1)$$

with y_i being the rapidities of the heavy quarks, y is the inelasticity variable, $x_B = Q^2/(2P \cdot q)$, where $Q^2 = -q^2 = -(\ell - \ell')^2$ is the virtuality of the photon. The full expressions for $d\sigma^U$ and $d\sigma^T$ are given in Ref. [4]. The azimuthal modulations that provide access to $h_1^{\perp g}$ can be singled out by means of the following observables [5, 6]

$$|\langle \mathcal{W}(\phi_T, \phi_\perp) \rangle| = \left| \frac{\int d\phi_\perp d\phi_T \mathcal{W}(\phi_T, \phi_\perp) d\sigma}{\int d\phi_\perp d\phi_T d\sigma} \right| = \frac{\mathbf{q}_T^2}{2M^2} \frac{|h_1^{\perp g}(x, \mathbf{p}_T^2)|}{f_1^g(x, \mathbf{p}_T^2)} \mathcal{F}^{\mathcal{W}}(y, z, Q^2, M_\perp^2), \quad (3.2)$$

with $\mathcal{W}(\phi_T, \phi_\perp) = \cos 2\phi_T, \cos 2(\phi_T - \phi_\perp)$. Moreover, $z = P \cdot K_1 / P \cdot q$ and $M_\perp^2 = M_Q^2 + \mathbf{K}_\perp^2$, where M_Q is the mass of the heavy quark, while the functions $\mathcal{F}^{\mathcal{W}}$ are presented explicitly in Ref. [4].

On the other hand, in order to isolate the ϕ_S dependent terms related to the T -odd gluon TMDs, we define the azimuthal moments

$$A_N^{W(\phi_S, \phi_T)} \equiv 2 \frac{\int d\phi_T d\phi_\perp W(\phi_S, \phi_T) [d\sigma(\phi_S, \phi_T, \phi_\perp) - d\sigma(\phi_S + \pi, \phi_T, \phi_\perp)]}{\int d\phi_T d\phi_\perp [d\sigma(\phi_S, \phi_T, \phi_\perp) + d\sigma(\phi_S + \pi, \phi_T, \phi_\perp)]}. \quad (3.3)$$

After integration over ϕ_\perp , only three independent modulations are left: $\sin(\phi_S - \phi_T)$, $\sin(\phi_S + \phi_T)$, $\sin(\phi_S - 3\phi_T)$, each one related to a different T -odd gluon TMD. These angular structures and the TMDs they probe are very similar to the case of quark asymmetries in SIDIS, $ep^\uparrow \rightarrow e'hX$, with ϕ_T replaced by ϕ_h [10]. The same holds for the $\cos 2(\phi_T - \phi_\perp)$ asymmetry in Eq. (3.2). More

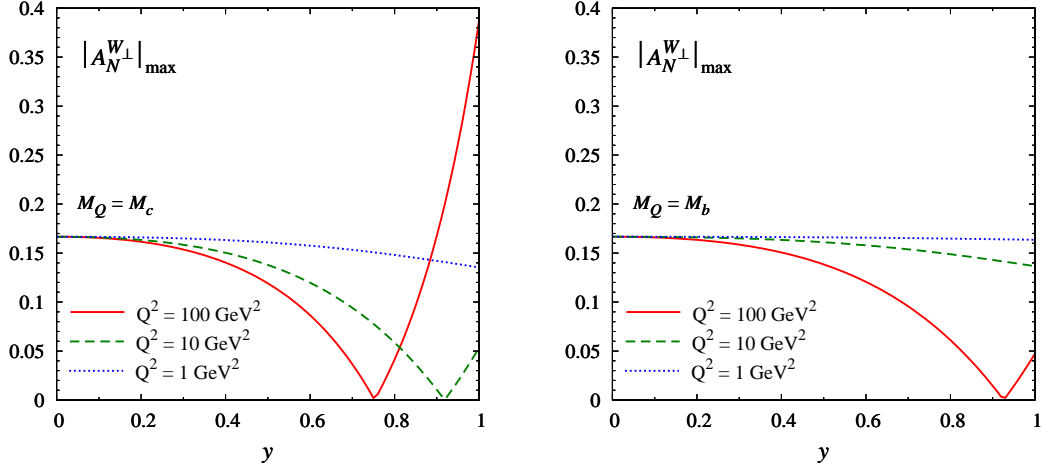


Figure 2: Same as in Fig. 1, but for the upper bounds $|A_N^W|_{\max}$ of $A_N^{\sin(\phi_S^\perp + \phi_T^\perp)}$ and $A_N^{\sin(\phi_S^\perp - 3\phi_T^\perp)}$.

explicitly, we obtain:

$$A_N^{\sin(\phi_S - \phi_T)} = \frac{|\mathbf{q}_T|}{M_p} \frac{f_{1T}^{\perp g}(x, \mathbf{q}_T^2)}{f_1^g(x, \mathbf{q}_T^2)}, \quad (3.4)$$

$$A_N^{\sin(\phi_S + \phi_T)} = \frac{|\mathbf{q}_T|}{M_p} \frac{h_1^g(x, \mathbf{q}_T^2)}{f_1^g(x, \mathbf{q}_T^2)} \mathcal{F}^{\sin(\phi_S + \phi_T)}(y, z, Q^2, M_\perp^2), \quad (3.5)$$

$$A_N^{\sin(\phi_S - 3\phi_T)} = -\frac{|\mathbf{q}_T|^3}{2M_p^3} \frac{h_{1T}^{\perp g}(x, \mathbf{q}_T^2)}{f_1^g(x, \mathbf{q}_T^2)} \mathcal{F}^{\sin(\phi_S - 3\phi_T)}(y, z, Q^2, M_\perp^2), \quad (3.6)$$

where $\mathcal{F}^{\sin(\phi_S + \phi_T)} = \mathcal{F}^{\sin(\phi_S - 3\phi_T)} = \mathcal{F}^{\cos 2\phi_T} \equiv \mathcal{F}$. Note that $\langle \cos 2\phi_T \rangle$, $A_N^{\sin(\phi_S + \phi_T)}$ and $A_N^{\sin(\phi_S - 3\phi_T)}$ vanish in the limit $y \rightarrow 1$, which for $s/Q^2 \rightarrow \infty$ corresponds to the limit $x \rightarrow 0$, since $\mathcal{F} \rightarrow 0$ when $y \rightarrow 1$. Furthermore, a measurement of the ratio

$$\frac{A_N^{\sin(\phi_S - 3\phi_T)}}{A_N^{\sin(\phi_S + \phi_T)}} = -\frac{\mathbf{q}_T^2}{2M_p^2} \frac{h_{1T}^{\perp g}(x, \mathbf{q}_T^2)}{h_1^g(x, \mathbf{q}_T^2)} \quad (3.7)$$

would probe directly the relative magnitude of $h_{1T}^{\perp g}$ and h_1^g without dependences on any of the other kinematic variables in the process. From the positivity bounds in Eqs. (2.5), we find that the maximal value of the Sivers asymmetry in Eq. (3.4) is always one, while $\langle \cos 2\phi_T \rangle$ and the asymmetries in Eqs. (3.5) and (3.6) have the same upper bounds, that we denote by A_N^W . The maximal values of $|A_N^W|$ are shown in Fig. 1 as a function of y in the kinematic region specified in the caption. In this and subsequent numerical analyses we take $M_c = 1.3$ GeV and $M_b = 4.2$ GeV.

Alternatively, the azimuthal angles can be defined w.r.t. ϕ_\perp instead of ϕ_ℓ , that can be integrated over. In analogy to Eqs. (3.4)-(3.6), we get

$$A_N^{\sin(\phi_S^\perp - \phi_T^\perp)} = \frac{|\mathbf{q}_T|}{M_p} \frac{f_{1T}^{\perp g}}{f_1^g}, \quad A_N^{\sin(\phi_S^\perp + \phi_T^\perp)} = \frac{|\mathbf{q}_T|}{M_p} \frac{h_1^g}{f_1^g} \mathcal{F}^\perp, \quad A_N^{\sin(\phi_S^\perp - 3\phi_T^\perp)} = -\frac{|\mathbf{q}_T|^3}{2M_p^3} \frac{h_{1T}^{\perp g}}{f_1^g} \mathcal{F}^\perp, \quad (3.8)$$

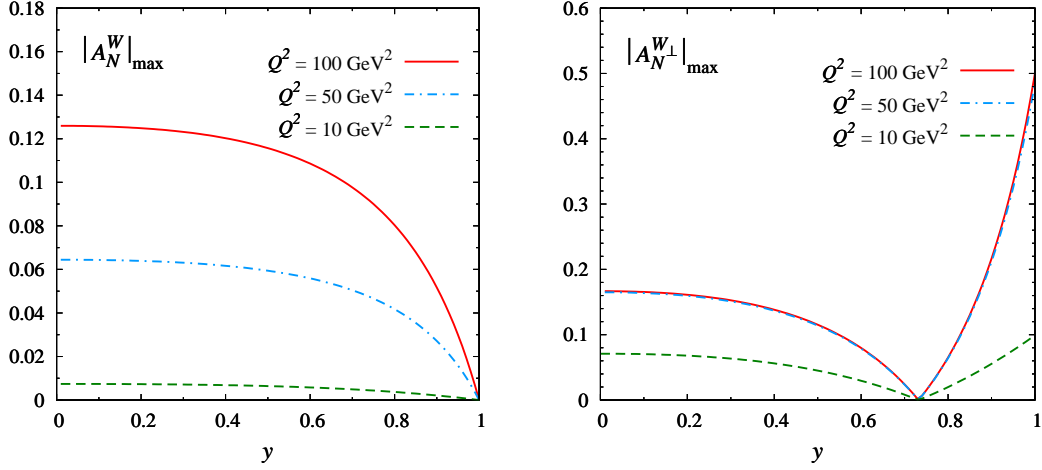


Figure 3: Upper bounds $|A_N^W|_{\max}$, with $W = \sin(\phi_S + \phi_T)$, $\sin(\phi_S - 3\phi_T)$ (left panel), and $|A_N^{W_\perp}|_{\max}$, with $W_\perp = \sin(\phi_S^\perp + \phi_T^\perp)$, $\sin(\phi_S^\perp - 3\phi_T^\perp)$ (right panel), for the process $ep \rightarrow e'\text{jetjet}X$. Estimates are given as a function of y , at different values of $K_\perp \geq 4$ GeV (chosen in such a way that the asymmetries are maximal) and Q^2 , with $z = 0.5$.

where $\mathcal{F}^\perp = \mathcal{F}^{\cos 2(\phi_T - \phi_\perp)}$, see Eq. (3.2). As a consequence, $\langle \cos 2(\phi_T - \phi_\perp) \rangle$ has the same upper bound of $A_N^{\sin(\phi_S^\perp + \phi_T^\perp)}$ and $A_N^{\sin(\phi_S^\perp - 3\phi_T^\perp)}$, named $A_N^{W_\perp}$ and presented in Fig 2. We note that the upper bounds of $A_N^{W_\perp}$ do not vanish when $y \rightarrow 1$, therefore these asymmetries are more suitable than A_N^W for small- x studies.

Turning now to the process $e(\ell) + p(P, S) \rightarrow e(\ell') + \text{jet}(K_1) + \text{jet}(K_2) + X$, its cross section at LO receives contributions from two partonic channels: $eq \rightarrow e'qg$ and $eg \rightarrow e'q\bar{q}$. The angular structure of the cross section is the same as the one for heavy quark pair production given in Eq. (3.1). In a kinematic region where x is small enough, the quark contribution can be neglected and the maximal values of the asymmetries for dijet production will be the same as the ones for heavy quark pair production in the limit of massless quarks. These upper bounds for the T -odd gluon TMD asymmetries are shown in Fig. 3, where we have selected $K_\perp \geq 4$ GeV [4].

4. Process dependence of gluon TMDs

The subprocesses $\gamma^* g \rightarrow Q\bar{Q}$ and $\gamma^* g \rightarrow q\bar{q}$, contributing respectively to heavy quark pair and dijet production, probe the gluon correlator in Eq. (2.4) with two future pointing gauge links, which are referred to as $+$ links as well. The TMDs extracted from these processes can be related to the ones probed in specific pp reactions. For instance, in $pp \rightarrow \gamma\gamma X$ [11] one can access gluon TMDs with two past-pointing Wilson lines. Therefore, we predict the following relation for the gluon Sivers functions:

$$f_{1T}^{\perp g[e p^\dagger \rightarrow e' Q\bar{Q}X]}(x, p_T^2) = -f_{1T}^{\perp g[p^\dagger p \rightarrow \gamma\gamma X]}(x, p_T^2), \quad (4.1)$$

and the same holds for the other two T -odd gluon TMDs, h_1^g (or h_{1T}) and h_{1T}^\perp . This can be considered as the gluon analogue of the sign change relation between the quark Sivers function probed in SIDIS and Drell-Yan. In contrast, since T -even gluon TMDs with two $-$ links are equal to those

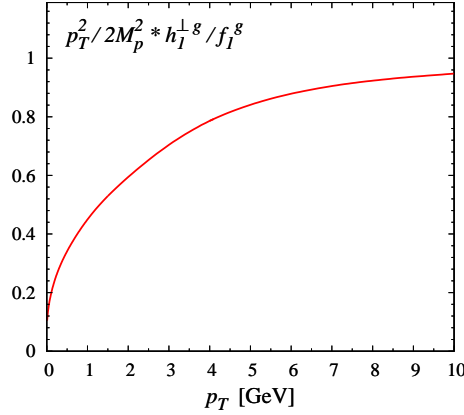


Figure 4: Ratio of the WW-type gluon TMDs $h_1^{\perp g}$ and f_1^g in the MV model as a function of p_T .

with two $+$ links, it should be

$$h_1^{\perp g [ep \rightarrow e' Q\bar{Q}X]}(x, p_T^2) = h_1^{\perp g [pp \rightarrow \gamma\gamma X]}(x, p_T^2). \quad (4.2)$$

Similar conclusions can be drawn if, instead of $\gamma\gamma$, one considers any other color-singlet final state in gg -dominated kinematics, such as a $J/\psi - \gamma$ pair [12], a (pseudo)scalar quarkonium [13], or even a Higgs boson [14]. This provides additional motivation to study gluon TMDs at RHIC or AFTER@LHC and compare them to EIC studies in the future.

On the other hand, by looking at the process $pp \rightarrow \gamma\text{jet}X$ in the kinematic regime dominated by gluons inside one of the protons, the subprocess $qg \rightarrow \gamma q$ can be selected, which probes gluon TMDs with future and past pointing Wilson lines, *i.e.* a $+$ and $-$ link. Hence the two processes $ep \rightarrow e' Q\bar{Q}X$ and $pp \rightarrow \gamma\text{jet}X$ probe distinct and entirely independent gluon TMDs, which cannot be related to each other. We conclude that TMD observables accessible at the LHC and at EIC can be either related or complementary depending on the process.

5. Gluon TMDs and azimuthal asymmetries in the small- x region

The gluon TMDs that can be accessed in heavy quark and dijet production in DIS, characterized by two $+$ gauge links, correspond to the so-called Weizsäcker-Williams (WW) distributions at small x [15, 16], while those with a $+$ and a $-$ link correspond to dipole distributions. Both the WW and the dipole linearly polarized gluon distributions can be calculated using saturation models, since they have the same $\ln 1/x$ enhancement as the unpolarized TMDs in the small- x region. For example, the ratio between the WW linearly polarized and unpolarized gluon TMDs in a McLerran-Venugopalan (MV) model [17] is given by [18, 19, 4]

$$\frac{\mathbf{p}_T^2}{2M_p^2} \frac{h_1^{\perp g}(x, \mathbf{p}_T^2)}{f_1^g(x, \mathbf{p}_T^2)} = \frac{\int_0^\infty \frac{dr_\perp}{r_\perp} J_2(|\mathbf{p}_T|r_\perp) \ln^{-1} \left[\frac{1}{r_\perp^2 \Lambda_{QCD}^2} + e \right] \left\{ 1 - e^{-\frac{r_\perp^2 Q_{s0}^2}{4} \ln \left[\frac{1}{r_\perp^2 \Lambda_{QCD}^2} + e \right]} \right\}}{\int_0^\infty \frac{dr_\perp}{r_\perp} J_0(|\mathbf{p}_T|r_\perp) \left\{ 1 - e^{-\frac{r_\perp^2 Q_{s0}^2}{4} \ln \left[\frac{1}{r_\perp^2 \Lambda_{QCD}^2} + e \right]} \right\}}, \quad (5.1)$$

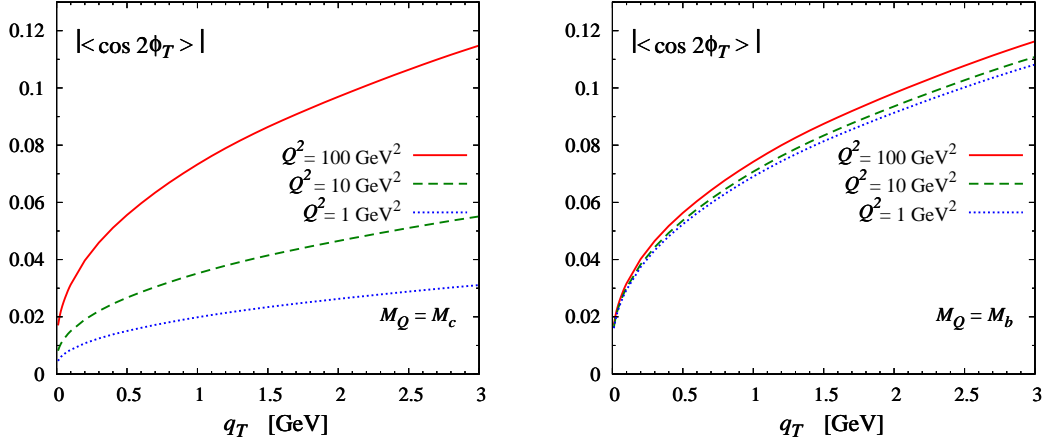


Figure 5: $|\langle \cos 2\phi_T \rangle|$ asymmetry in the MV model, as a function of $q_T \equiv |\mathbf{q}_T|$, calculated at $|\mathbf{K}_\perp| = 6$ GeV, $z = 0.5$, $y = 0.1$ and at different values of Q^2 , for $ep \rightarrow e'c\bar{c}X$ (left panel) and $ep \rightarrow e'b\bar{b}X$ (right panel).

where Q_{s0} is the saturation scale, which has to be extracted from fits to experimental data. This ratio is shown in Fig. 5 for the $Q_{s0}^2 = 0.35$ GeV² at $x = 0.01$ and $\Lambda_{QCD} = 0.2$ GeV. It turns out that this ratio is not saturated for p_T values below 10 GeV, although it is still sizable except for very small p_T values. This is in contrast with the dipole case, in which such ratio is always saturated [18]. Using the MV model expression in Eq. (5.1), we show in Figs. 5 and 6 our estimates for the absolute values of $\langle \cos 2\phi_T \rangle$ and $\langle \cos 2(\phi_T - \phi_\perp) \rangle$, respectively, in two different kinematic regions. Both asymmetries are sizable and decrease for values of y and $|\mathbf{K}_\perp|$ larger than the ones chosen. Note that the center of mass energy has to be sufficiently large for these curves to be in the small- x range. For an EIC, the planned \sqrt{s} varies from about 20 to 150 GeV [7], hence $x_B = Q^2/ys < 0.01$ for $y \geq 0.1$ requires $Q^2 < (10^{-3} - 10^{-2})s$. For $\sqrt{s} = 60$ GeV the $Q^2 = 100$ GeV² curve should not be considered. The large Q^2 curves are included for a high energy EIC or for an analysis of HERA data, for which $\sqrt{s} = 320$ GeV.

Turning to the small- x behavior of the WW-type T -odd gluon TMDs, this can be perturbatively computed at large p_T following the standard collinear twist-3 approach [20]. Such studies suggest that the WW T -odd distributions are suppressed by a factor of x as compared to the corresponding dipole ones. The complete expressions for their sub-asymptotic behavior, which cannot be estimated in the MV model, are given in Ref. [4], where three different models for the WW gluon TMDs have also been proposed. The ratio of asymmetries in Eq. (3.7) could be used to test such models, because each one of them leads to a different prediction for the ratio.

6. Conclusions

Azimuthal asymmetries in heavy quark pair and dijet production in DIS processes could provide direct access to gluon TMDs. These asymmetries are very similar to the ones measured in semi-inclusive DIS in order to extract quark TMDs. We have identified the kinematic regions in which they are maximal and found that, in such domains, the corresponding upper bounds are siz-

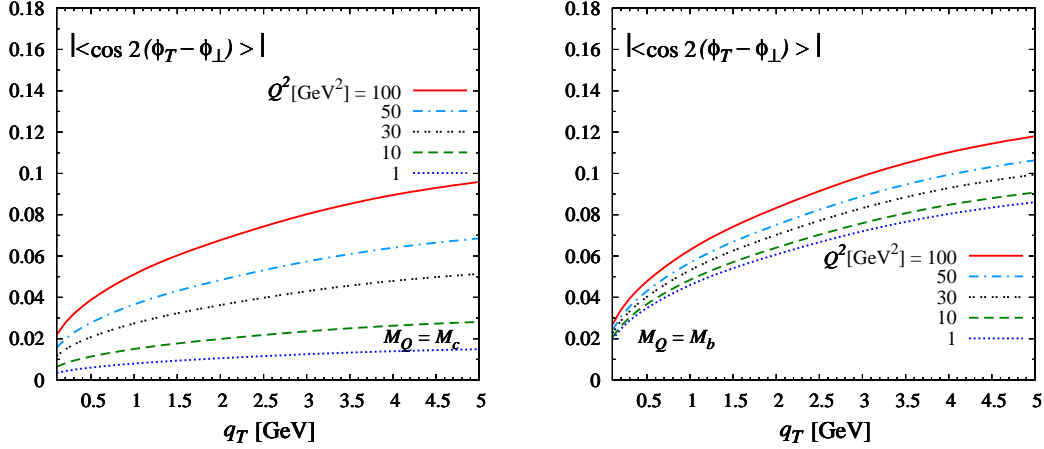


Figure 6: $|\langle \cos 2(\phi_T - \phi_\perp) \rangle|$ asymmetry in the MV model, as a function of $q_T \equiv |\mathbf{q}_T|$, calculated at $|\mathbf{K}_\perp| = 10$ GeV, $z = 0.5$, $y = 0.3$, and different values of Q^2 , for $ep \rightarrow e'c\bar{c}X$ (left panel) and $ep \rightarrow e'b\bar{b}X$ (right panel).

able. Their measurements at an EIC would allow to test our prediction of the sign change of the T -odd gluon TMDs by comparison with the corresponding observables at RHIC and AFTER@LHC.

In the small- x region, the TMDs under investigation correspond to the WW-type gluon distributions. Although the WW linearly polarized gluon distribution, unlike the dipole one, does not saturate the positivity bound, its effects in heavy quark pair and dijet production at an EIC should still be measurable, as it turns out from our analysis in the framework of the MV model. Saturation models cannot be used to estimate the T -odd WW gluon TMDs because their asymptotic behavior at small- x vanishes. Nevertheless, we propose to look at the ratio of the $\sin(\phi_S + \phi_T)$ and $\sin(\phi_S - 3\phi_T)$ modulations, for which other model expectations are provided [4], to probe two of the T -odd TMDs. It will be interesting to check experimentally the theoretical prediction of different asymptotic behavior at small x of the WW and dipole type T -odd gluon TMDs. The latter ones could be probed in other processes, such as virtual photon plus jet production in polarized proton-proton collisions at RHIC. To conclude, the studies of azimuthal asymmetries in heavy quark pair and dijet production could form a prominent part of both the spin and the small- x physics programs at a future EIC.

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